

## Q, F and H

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- Definitions:  $F = P_{\alpha} / (P_{\alpha} + P_{ext})$        $Q = 5 P_{\alpha} / P_{ext}$
- Hence  $F = Q / (Q + 5)$  and  $Q = 5 F / (1 - F)$
- $F =$  “fraction of self heating” is a physics variable. We need  $F > 0.5$  ( $Q=5$ ) or  $0.66$  ( $Q=10$ ) and as  $F \rightarrow 1$ ,  $Q$  gets very large.  $F$  is a less sensitive variable and we really should focus on  $F$
- $Q$  is an “energy economics variable” and if we ever get in the range  $5 < Q < 10$  we can tweak it higher.
- Relation to  $H$ : the H-mode or L-mode confinement time enhancement factor.

$$P_{\alpha} \propto V n^2 T^2 \text{ high } T \quad (\text{or } V n^2 T^2 (T/10) \text{ low } T)$$

$$\propto n T W = n T \tau (P_{\alpha} + P_{ext}) \quad \text{ignoring } P_{brem} \text{ at very low } T$$

hence  $F \propto n T \tau$  the “fusion product”

$$\text{typically (at fixed } B, a, R/a, q \text{ etc)} \quad \tau \propto H (P_{\alpha} + P_{ext})^{-1/3}$$

$$\text{and } n T \propto H (P_{\alpha} + P_{ext})^{2/3}$$

$$\text{so } F \propto H^2 (P_{\alpha} + P_{ext})^{1/3} \quad \text{or} \quad F \propto H^2 [P_{ext} / (1-F)]^{1/3}$$

$H = 1.15$  (like top of RMSE =15%) means  $F$  increases by 30%

or  $F=0.5$  ( $Q=5$ ) goes to  $F=0.66$  ( $Q=10$ )     $H=0.85$  is not reported     $H = 1.15$  is front page

- And higher sensitivities are possible.....suppose in low T regime

$$P_{\alpha} \propto T^3 \propto H^3 (P_{\alpha} + P_{\text{ext}})^2$$

$$F = H^3 [P_{\text{ext}} / (1-F)]$$

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